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## GENERATION OF DIFFUSE NON-THERMAL ATMOSPHERIC PLASMAS

### Field of the Invention

This invention relates to the generation of gas plasmas, and more particularly to the  
15 electrically-efficient production of diffuse non-thermal atmospheric gas plasmas.

### Review of the Art Known to the Applicant(s)

Nonthermal gas discharges generated at atmospheric pressure find widespread use for  
ozone production (see B. Eliasson and U. Kogelschatz, "Nonequilibrium volume  
20 plasma chemical-processing", *IEEE Trans. Plasma Science*, vol.19, pp. 1063 – 1077,  
1991), pollution control (see B. M. Penetrante, J. N. Barsley, and M. C. Hsaio, "Kinetic  
analysis of non-thermal plasmas used for pollution control", *Japan. J. Appl. Phys.* Vol.  
36, pp. 5007 – 5017, 1997.), and surface modification of Polymer films (see J.  
Friedrich, L. Wigant, W. Unger, A. Lippitz, and H. Wittrich, "Corona, spark and  
25 combined UV and ozone modification of polymer films WeBP23", *Surface & Coatings*

*Technology*, vol. 98, pp. 879 – 885, 1998.). Typically, such atmospheric plasmas consist of many nanosecond-scale microdischarges of streamer-like filaments (see A. C. Gentile and M. J. Kushner, “Reaction chemistry and optimization of plasma remediation of  $N_xO_y$  from gas streams”, *J. Appl. Phys.* vol.78, pp. 2074 – 2085, 1995.)

5 and much is known of their fundamental properties and their applications (see also M. Baeva, A. Dogan, J. Ehlbeck, A. Pott, and J. Uhlenbusch, “CARS diagnostic and modeling of a dielectric barrier discharge”, *Plasma Chem. Plasma Processing*, vol. 19, pp. 445 – 466, 1999 and R. Hackam and H. Akiyama, “Air pollution control by electrical discharges”, *IEEE Trans. Dielectrics and Electrical Insulation*, vol.7, pp.654

10 – 683, 2000.). More recently it has been suggested that nonthermal atmospheric gas discharges can also be diffuse and luminous with the duration of their discharge current pulses in excess of sub-milliseconds (see E. E. Kunhardt, “Generation of large-volume, atmospheric-pressure, nonequilibrium plasmas”, *IEEE Trans. Plasma Sci.*, vol.28, pp.189 – 200, 2000; M. J. Shenton and G. C. Stevens, “Surface modification of

15 polymer surfaces: atmospheric plasma versus vacuum plasma treatments”, *J. Physics. D: Appl. Phys.*, vol.34, pp. 2761 – 2768, 2001 and F. Massines, A. Rabehi, Ph Decomps, R. B. Gadri, P. Segur, and C. Mayoux, “Experimental and theoretical study of a glow discharge at atmospheric pressure controlled by dielectric barrier”, *Journal of Applied Physics*, vol.83, pp. 2950 – 2957, 1998.). Compared to their counterparts in the

20 streamer-dominated mode, these diffuse nonthermal atmospheric plasmas have greater spatial uniformity, better temporal stability, and much lower gas temperature, typically in the range 75°C – 150°C (see A. Schutze A, J. Y. Jeong, S. E. Babayan, J. Park, and G. S. Selwyn, “The atmospheric-pressure plasma jet: A review and comparison to other plasma sources”, *IEEE Trans Plasma Sci*, vol. 26, pp.1685 – 1694, 1998.). These

25 properties make them particularly attractive for a number of key materials processing

applications such as etching, deposition, and structural modification of polymeric surfaces. These diffuse nonthermal atmospheric plasmas have been generated with dielectrically insulated electrodes at audio frequencies (see Massines *et al, supra*), with un-insulated electrodes at radio frequencies (see Schutze *et al, supra*), and at  
5 microwave frequencies (see Shenton and Stevens, *supra*). Apart from their desirable spatial and temporal characteristics, diffuse nonthermal atmospheric plasmas have different electrical and chemical properties from that of their streamer-dominated counterparts. While many of their fundamental properties remain to be fully understood, the focus of research has been largely experimental improvement of  
10 existing applications and empirical exploration of new applications.

For controlled and optimised performance of material processing, it is always desirable to be able to adjust and tailor plasma properties. In the case of diffuse nonthermal atmospheric plasmas, this has been pursued mainly through plasma rig designs and gas composition, and to a lesser extent through an appropriate choice of  
15 excitation frequency (See J. Park, I. Henins, W. Hermann, and G. S. Selwyn, "Gas breakdown in an atmospheric pressure radio-frequency capacitive plasma source", *J. Appl. Phys.*, vol. 89 15 – 19, 2001).

US Patent number US6228330 teaches the use of atmospheric-pressure plasmas for the decontamination and sterilization of sensitive equipment and material, and provides  
20 evidence of their efficacy in inactivation of a number of bacterial spores. The patent describes a system for plasma recirculation, but discloses no shaping of the waveform of the applied voltage.

The European patent application number EP 1 040 839 describes a multi-stage process for sterilization using a gas plasma. The application discloses no shaping of the waveform of the applied voltage.

US Patent number 6,118,218 describes an atmospheric pressure plasma treater  
5 incorporating a porous metallic electrode. The application discloses no shaping of the waveform of the applied voltage.

A number of features of non-thermal gas plasmas are particularly important in regard to their applicability. First, the temperature of the gas plasma may be deleterious to objects with which the plasma comes into contact, for example during sterilization or  
10 surface decontamination. Second, the power dissipation in the plasma has a direct bearing on the energy efficiency of plasma generation, which is important for the overall economic efficiency of devices using the plasma, and is particularly important in applications remote from a readily-available supply of electrical power.

Accordingly, it is an object of the present invention to provide a means to generate  
15 atmospheric-pressure plasmas at increased energy efficiency and at low temperature, whilst retaining the desirable feature of a high density of active species.

### Summary of the Invention

In accordance with the inventive concept, these objects are addressed by the use of an  
20 applied voltage that exhibits a waveform (as defined herein) which is truncated (as herein defined) and/or which decays asymmetrically from its peak value.

Advantageously, the applied voltage,  $V$ , as a function of time,  $t$ , said time  $t$  being measured from any arbitrary instant, takes the form of a waveform,  $V(t)$ , of cycle time  $T$ , wherein in at least one of the half cycles, i.e. . between  $(t=i T)$  and  $(t=i T + T/2)$  or

between  $(t=iT + T/2)$  and  $(t=(i+1)T)$ , where  $i$  takes integer values, the waveform is characterised by the magnitude of the integral of the voltage with respect to time being greater in the first half of said half cycle than in the second half of said half cycle.

Advantageously also, the applied voltage,  $V$ , as a function of time,  $t$ , said time  $t$  being  
5 measured from any arbitrary instant, takes the form of a waveform,  $V(t)$ , of cycle time  $T$ , wherein in at least one of the half cycles, i.e. between  $(t=iT)$  and  $(t=iT + T/2)$  or between  $(t=iT + T/2)$  and  $(t=(i+1)T)$ , where  $i$  takes integer values, the waveform is characterised by a period of substantially constant voltage.

Also advantageously, the applied voltage may be defined by equation E1, below.

10 Also advantageously, the applied voltage may be defined by equation E2, below.

Also advantageously, the applied voltage may be defined by equation E3, below.

Preferably, the applied voltage may be generated by the action of a control system, said control system using a measurement of the plasma discharge current as an input signal.

Included within the scope of the invention is a method of generating a gas plasma  
15 substantially as described herein with reference to and as illustrated by the accompanying drawings.

### **Brief description of the Drawings**

Figure 1 is a graph showing the reduced ionization coefficient of argon as computed  
20 with a Boltzmann solver (circles) and with the source term technique (+) together with reduced ionization coefficient of nitrogen using the source term technique (solid line).

Figure 2 is a graph showing typical voltage-current characteristics of a helium-nitrogen discharge under sinusoidal excitation with the gas voltage in solid curve, the discharge current in thick dashed curve, and the applied voltage in dot curve.

Figure 3 is a graph showing a generalised peak-levelled waveform.

Figure 4 is a graph showing (a) A pulsed excitation voltage (solid curve) at 10kHz repetition frequency, made from a sinusoidal voltage (dashed curve) having its peaks levelled; and (b) time dependence of the peak-levelled excitation voltage (dot curve),  
5 the gas voltage (solid curve), and the discharge current (thick dashed curve).

Figure 5 is graph showing normalized plasma power density (circles) and normalized electron density (diamonds) as a function of reduced magnitude of the applied voltage with 0.5% nitrogen.

Figure 6 is a graph showing the normalized plasma power density (circles) and  
10 normalized electron density (diamonds) as a function of reduced magnitude of the applied voltage with no nitrogen impurities.

Figure 7 is a graph showing the normalized electron density (circles) and normalized metastable density (diamonds) as a function of reduced magnitude of the applied voltage with 0.5% nitrogen impurities.

15 Figure 8 is a graph showing a generalised tail-trimmed waveform.

Figure 9 is a graph showing (a) a peak-levelled excitation voltage at 10kHz repetition frequency (dashed curve) and with its pulse tail trimmed (solid curve); and (b) time dependence of the peak-levelled and tail-trimmed excitation voltage (dot curve), the gas voltage (solid curve), and the discharge current (thick dashed curve).

20 Figure 10 is a graph showing (a) a sinusoidal excitation voltage at 10kHz repetition frequency (dashed curve) and with its tail shaped with a Gaussian decay (solid curve); and (b) time dependence of the excitation voltage (dot curve), the gas voltage (solid curve), and the discharge current (thick dashed curve).

### The Inventive Concept

The inventive concept considers pulsing plasma excitation voltage as a way to control and improve properties of diffuse nonthermal atmospheric plasmas. For streamer-dominated atmospheric gas discharges, pulsed plasma generation has been known to facilitate better energy efficiency and greater control of the glow-to-arc transition although this has never been achieved for diffuse, nonthermal atmosphere plasmas. If similar improvements could be achieved for such plasmas, it would be useful for applications where plasma power consumption is an important issue, for example aircraft cloaking and industry-scale surface treatment.

To illustrate the benefits of plasma pulsing in different plasma generation configurations, we will consider nonthermal atmospheric gas discharges generated in a helium-nitrogen mixture and between two dielectrically insulated parallel-plate electrodes. Specifically the inventive concept attempts to answer (1) whether pulsed plasma generation can lead to saving in electrical power needed to sustain the generated plasma; and (2) if so how pulse shape and width may be adjusted to enhance energy efficiency. The approach uses on a one-dimensional computer code (See X. T. Deng and M. G. Kong, "Parametric conditions for generation of stable atmospheric pressure nonthermal plasmas", in the *2001 Annual Report, Conference on Electrical Insulation and Dielectric Phenomena* 677 (IEEE Catalogue Number: 01CH37225), pp. 677 – 680, 2001) developed using a hydrodynamic model similar to those employed in most numerical studies for diffuse nonthermal atmospheric plasmas (See Massines *et al*, *supra* and F. Tochikubo, T. Chiba, and T. Watanabe, "Structure of low-frequency helium glow discharge at atmospheric pressure between parallel plate dielectric

electrodes", *Japanese Journal of Applied Physics*, vol. 38, pp. 5244 – 5250, 1999). The key features of the underlying model of diffuse nonthermal atmospheric plasmas as well as its numerical implementation will be described below, for clarity. Voltage-current characteristics of nonthermal atmospheric plasma under sinusoidal excitation  
5 will be used as an example to demonstrate the utility of this approach.

#### *A physical model of nonthermal atmospheric plasmas*

Diffuse nonthermal atmospheric plasmas may be induced and sustained between two parallel-plate electrodes, each one optionally coated with a dielectric layer and  
10 connected externally to a sinusoidal voltage source, typically at voltages in excess of 1kV, and at audio frequencies. The background gas is, for example, atmospheric helium mixed with a small fraction of nitrogen (up to 1%) at room temperature of 293K, and the dynamics of the generated nonthermal atmospheric plasma is described by the Boltzmann equation, well known in the art. It has been established that the  
15 hydrodynamic assumptions can be applied to diffuse nonthermal atmospheric plasmas (See Massines *et al* and Tochikubo *et al*, *supra*). This reduces the Boltzmann equations to the continuity and momentum transfer equations for electrons and ions, thus facilitating a macroscopic description of plasma dynamics without its microscopic details. On the other hand, the dynamics of electrons and ions are determined by the  
20 electric field in the space between the two parallel electrodes, which has two components, one induced by the externally applied excitation voltage and the other by space charges. The electric field can be calculated by solving Poisson's equation. In the one-dimensional limit, the Boltzmann equations and Poisson's equations are closely coupled together as follows



$$\frac{\partial n_{\pm}}{\partial t} = S_{\pm}(r, t) - \frac{\partial [n_{\pm}(r, t)W_{\pm}(r, t)]}{\partial r} + \frac{\partial^2 [n_{\pm}(r, t)D_{\pm}(r, t)]}{\partial r^2} \quad (1a)$$

$$\frac{\partial n_i}{\partial t} = S_i(r, t) - \frac{\partial [n_i(r, t)W_i(r, t)]}{\partial r} + \frac{\partial^2 [n_i(r, t)D_i(r, t)]}{\partial r^2} \quad (1b)$$

$$\frac{\partial E(r, t)}{\partial r} = \frac{|e|}{\epsilon_0} [n_+(r, t) - n_-(r, t)] \quad (1c)$$

where  $n_+$  and  $n_-$  are the ion and electron densities respectively, and  $n_i$  is the density of the  $i^{\text{th}}$  neutral species considered.  $S_{\pm}$  and  $S_i$  are the source terms for charged particles and neutral species respectively.  $D$  and  $W$  are diffusion coefficient and drift velocity with subscripts  $-$ ,  $+$ , and  $i$  denoting respectively electrons, ions, and  $i^{\text{th}}$  neutral species considered in the physical model.  $E$  is the electric field,  $|e|$  is the charge of the electron,  $\epsilon_0$  is the dielectric permittivity, and  $r$  is the variable representing the spatial position normal to the electrode. With the hydrodynamic assumptions, reaction rate coefficients, ionization coefficients, drift velocity, and diffusion coefficients can be approximated as a function of the electric field in the ionised gas between the two electrodes. Thus this physical model is similar to those used in Massines *et al* (*supra*) and Tochikubo *et al*, (*supra*). The values of these coefficients are obtained from relevant experiments and several rate compilation studies which will be discussed in greater detail below. These allow eqs.(1a) and (1b) to be solved to yield densities of electrons, ionic species, and metastables, which then allows through eq.(1c) calculation of electric field. Boundary conditions between the ionized gas and the dielectrically coated electrodes need to be carefully treated. To this end, a circuit equation is included to relate the electric field in the gas to the source voltage (the output voltage of the power supply) via a source resistor,  $R_s$ , and two serial capacitors each representing one dielectric coating layer. The numerical algorithm used to solve the above equations is essentially based on the

Patankar scheme, and the discretization employs the upwind scheme (see S. Patankar, "Numerical heat transfer and fluid flow", Hemisphere publishing Co, 1980).

The model considers reactions involving eight different species, namely (1) two ground-state neutral species, He( $1^1S$ ) and N<sub>2</sub>( $4^0S$ ); (2) two helium metastables, He( $2^3S$ ) and He( $2^1S$ ); (3) electrons; (4) ground-state atomic helium ions, He<sup>+</sup>; (5) ground-state molecular helium ions, He<sub>2</sub><sup>+</sup> ( $2^3\Sigma_u^+$ ); and (6) ground state molecular nitrogen ions, N<sub>2</sub><sup>+</sup>. In total, the model considers 17 reactions, as detailed in Table 1 below, together with their reaction rates and reference sources. Products of these 17 reactions include two additional species, namely excited molecular helium (He<sup>\*</sup>) and atomic nitrogen (N). Any subsequent reaction of these two additional species with the original eight species is not considered in the model. It is worth noting that the model is capable of evaluating production of molecular nitrogen ions that are not considered in reported numerical studies of diffuse nonthermal atmospheric discharges (e.g. Massines *et al*, *supra* and Tochikubo *et al*, *supra*).

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**Table 1: Reactions considered for a He-N<sub>2</sub> discharge and their rate coefficients**

No	Reaction	Reaction rate	Reference
Direct ionization			
1	He + e → He <sup>+</sup> + e + e	$\alpha_1$	1, 2, 3
2	N <sub>2</sub> + e → N <sub>2</sub> <sup>+</sup> + e + e	$\alpha_2$	1, 4
Excitation			
3	He + e → He ( $2^3S$ ) + e	$\beta_1$	5
4	He + e → He ( $2^1S$ ) + e	$\beta_2$	5
5	He ( $2^3S$ ) + 2He ( $1^1S$ ) → He <sub>2</sub> <sup>*</sup> + He ( $1^1S$ )	$1.9 \times 10^{-34} \text{ cm}^6/\text{s}$	6
De-excitation			
6	He ( $2^3S$ ) + e → He ( $1^1S$ ) + e	$4.2 \times 10^{-9} \text{ cm}^3/\text{s}$	7
Penning ionisation			
7	He ( $2^3S$ ) + N <sub>2</sub> → He ( $1^1S$ ) + N <sub>2</sub> <sup>+</sup> + e	$8 \times 10^{-11} \text{ cm}^3/\text{s}$	5, 8
Stepwise ionisation			

No	Reaction	Reaction rate	Reference
8	$\text{He } (2^3\text{S}) + \text{He } (2^3\text{S}) \rightarrow \text{He } (1^1\text{S}) + \text{He}^+ + \text{e}$	$2.9 \times 10^{-9} \text{ cm}^3/\text{s}$	9
Charge transfer			
9	$\text{He}^+ + 2\text{He } (1^1\text{S}) \rightarrow \text{He}_2^+ + \text{He } (1^1\text{S})$	$6.3 \times 10^{-32} \text{ cm}^6/\text{s}$	13, 5
Recombination			
10	$\text{He}^+ + \text{e} \rightarrow \text{He } (1^1\text{S})$	$2 \times 10^{-12} \text{ cm}^3/\text{s}$	10
11	$\text{He}_2^+ + \text{e} \rightarrow \text{He}_2^*$	$5 \times 10^{-16} \text{ cm}^3/\text{s}$	11
12	$\text{He}^+ + \text{e} + \text{He} \rightarrow \text{He } (1^1\text{S}) + \text{He } (2^3\text{S})$	$1 \times 10^{-27} \text{ cm}^6/\text{s}$	10
13	$\text{He}_2^+ + 2\text{e} \rightarrow \text{He } (1^1\text{S}) + \text{e}$	$7.1 \times 10^{-20} \text{ cm}^6/\text{s}$	13, 5
14	$\text{He}_2^+ + \text{e} \rightarrow 2\text{He } (2^3\text{S}) + \text{He}$	$5 \times 10^{-9} \text{ cm}^3/\text{s}$	6
15	$\text{He}_2^+ + \text{e} + \text{He} \rightarrow \text{He}_2^* + \text{He}$	$5 \times 10^{-27} \text{ cm}^6/\text{s}$	11
16	$\text{N}_2^+ + \text{e} \rightarrow \text{N} + \text{N}$	$4.8 \times 10^{-8} \text{ cm}^3/\text{s}$	8
17	$\text{N}_2^+ + 2\text{e} \rightarrow \text{N}_2 + \text{e}$	$1.4 \times 10^{-26} \text{ cm}^6/\text{s}$	12

### References cited in Table 1

- (1) F. Massines *et al* (*supra*)
- (2) A. L. Ward, "Calculations of cathode-fall characteristics", Journal of Applied Physics, vol. 33, pp. 2789 – 2794, 1964.
- (3) J. Dutton, "A survey of electron swarm data", J. Phys Chem. Ref. Data, vol.4, pp. 577 – 856, 1975.
- (4) I. Peres, N. Ouadoudi, L. C. Pitchford, and J. P. Boeuf, "Analytical formulation of ionization source term for discharge models in argon, helium, nitrogen, and silane", J. Appl. Phys., vol.72, pp. 4533 – 4536, 1992.
- (5) R. Ben Gadri, "Numerical simulation of an atmospheric pressure and dielectric barrier controlled glow discharge", PhD thesis, University Paul Sabatier of Toulouse, France, 1997.
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  - (10) T. Quinteros, H. Gao, D. R. DeWitt, R. Schuch, S. Pajek, S. Asp, and D. Belkic, "Recombination of D<sup>+</sup> and He<sup>+</sup> ions with low energy free electrons", *Phys. Rev. A*, vol.51, pp. 1340 – 1346, 1995.
  - (11) P. C. Hill and P. R. Herman, "Reaction processes in a He<sub>2</sub><sup>+</sup>(<sup>2</sup>Π<sub>u</sub> → a<sub>2</sub>Σ<sub>g</sub><sup>+</sup>) flash lamp", *Phys. Rev. A.*, vol.47, pp. 4837 – 4844, 1993.
  - (12) I. A. Kossyl, A. Yu Kostinsky, A. A. Matveyev, and V. P. Silakov, "Kinetic scheme of the non-equilibrium discharge in nitrogen-oxygen mixtures", *Plasma Source Science and Tech*, vol.1, pp. 207 – 220, 1992.
  - (13) Tochikubo *et al*, (*supra*).
- 20 Ionization coefficients in helium can be evaluated using Ward's formula (A. L. Ward, *supra*) or experimental data compiled by Dutton (*supra*). Both agree well with those used in Massines *et al* (*supra*), particularly at large reduced electric field (>50Td). Our model uses Ward's formula. On the other hand, it is known from spectroscopic measurements that discharge dynamics in atmospheric helium is very strongly affected
- 25 by the presence of impurities, particularly nitrogen. For diffuse nonthermal atmospheric

helium discharges, the presence of nitrogen impurities has been either ignored or implemented with its ionization coefficient approximated by that of argon. Since argon has a greater ionization coefficient than nitrogen, the approximation of using argon ionization coefficient overestimates the ionization of nitrogen impurities. To this end, we note that it is possible to formulate analytically ionization source terms for discharges in argon, helium, and nitrogen (See Peres, *supra*). Thus under the same conditions

$$\frac{\alpha_A}{\alpha_B} = \frac{\text{ionization source term for species } A}{\text{ionization source term for species } B} \quad (2)$$

where  $\alpha$  is Townsend's first ionization coefficient with its subscript  $A$  and  $B$  indicating respectively species  $A$  and  $B$ . If species  $A$  is argon and species  $B$  is helium, the above formula can be used to predict the ionization coefficient of argon from that of helium as calculated from Ward's formula. As shown in Figure 1, the argon ionization coefficient calculated with this technique, indicated by crosses 1 leads to an excellent agreement with that computed using a Boltzmann solver (see Massines *et al*, *supra*), indicated by circles 2. Therefore equation 2 offers a simple yet reliable way to estimate the ionization coefficient of one gas from the known ionization coefficient of a reference gas. Similarly if we assume species  $A$  is nitrogen and  $B$  is helium, the ionization coefficient of nitrogen is obtained and this is shown in Figure 1, indicated by the solid line 3, as a function of the reduced electric field. The ionization coefficient thus calculated is used in our model for nitrogen (reaction #2 in Table 1). For excitation coefficients, we use that employed by Ben Gadri (*supra*). Similarly our model employs the same data used by Ben Gadri (*supra*) for diffusion coefficients and drift velocity. By way of example, and demonstration of the utility of the model presented above to

accurately and correctly predict the evolution and properties of atmospheric diffuse nonthermal gas plasmas, a simulation is now presented, as follows.

In this example, we consider a system with the two electrodes having a common radius  
5 of 2cm and separated with a gap fixed at 0.5cm. The total capacitance of the dielectric coatings on the two parallel-plate electrodes is 70pF, and the source resistor in the external circuit is 50 $\Omega$ . In this reference case, we consider a sinusoidal source voltage at 10kHz with a peak voltage of 1.5kV. Before the power supply is switched onto the plasma rig, the two electrodes are charged at 950V and so the initial gas voltage is  
10 950V. The background gas is 99.5% helium with 0.5% nitrogen unless otherwise stated, and its breakdown voltage is assumed to be 1.1kV, similar to the choice in Massines *et al (supra)*. The secondary electron emission coefficient is dependent on the surface condition of electrodes and as such it is not possible to choose a reliable coefficient that is applicable to most cases. Numerically different secondary emission  
15 coefficients in the 0.01 – 0.2 range affect the peak value of the discharge current. For numerical studies considered here, we choose 0.2 for atomic helium ions, 0.1 for molecular helium ions, and 0.01 for nitrogen ions (see A. von Engel, “*Ionized Gases*”, Chapter 3, reprinted by *American Institute of Physics*, 1994). Our numerical model assumes that diffuse nonthermal atmospheric plasma is established if its voltage and  
20 current are continuous and repetitive over at least 10 cycles of the applied voltage signal. Noting that discharge currents of both thermal plasmas and streamer-dominated nonthermal atmospheric plasmas tend to exhibit microscopic current pulses in tens nanosecond or less, pulse duration of the discharge current is an additional indicator for diffuse atmospheric plasmas. Figure 2 shows a plot of the applied voltage 4, the gas  
25 voltage 5, and the discharge current 6 as a function of time. Though not shown in

Figure 2, numerical results confirm that the discharge current 6 is in fact identical through many tens of cycles of the applied voltage 4 and so the discharge plasma is stable and repetitive temporally over a long period of time. The voltage-current characteristics are very similar to that obtained in a comparable experiment and its numerical simulation (Massines *et al, supra*), with a typical pattern of one discharge every half cycle of the applied voltage. Both gas voltage 5 and discharge current 6 exhibit very similar waveforms as those observed by Massines *et al (supra)* and Tochikubo *et al (supra)*. The peak discharge current 6 in Figure 2 is between 52 – 58 mA, lower than 90mA calculated by Massines *et al*. As shown in Figure 1, this may be partly due to the use of the larger ionization coefficient of argon used by Massines *et al* to approximate the nitrogen ionization coefficient. It is interesting to note that the peak current density of  $7.2\text{mA}/\text{cm}^2$  ( $=90\text{mA}/\pi 2^2$ ) is the highest reported for diffuse atmospheric helium discharges generated between dielectrically coated electrodes and at kilohertz frequencies. In a series of very similar experiments performed at Tennessee University, the peak current density is found at most  $1\text{mA}/\text{cm}^2$  (J. R. Roth, “*Industrial plasma engineering*”, Chapter 12, vol.1, *IoP publishing*, Bristol, 1995.). A similar peak current density of about  $0.4\text{mA}/\text{cm}^2$  ( $=11.25\text{mA}/\pi 3^2$ ) was measured with 3kHz plasma excitation by the Okazaki group at Sophia University in Japan (T. Yokoyama, M. Kogoma, T. Moriwaki, and S. Okazaki, “The mechanism of the sterilisation of glow plasmas at atmospheric pressure”, *J. Phys. D: Appl. Phys.*, vol. 23, pp. 1125 – 1128, 1990), whereas another Japanese group measured  $1.8\text{mA}/\text{cm}^2$  with a 100kHz power supply. More recently a helium discharge experiment performed at Minnesota University recorded a peak current density measured at  $0.5\text{mA}/\text{cm}^2$  with 15kHz driving voltage (L. Mangolini, K. Orlov, U. Kortshagen, H. Heberlein, and U. Kogelschatz, “Radial structure of low-frequency atmospheric-pressure glow discharge in helium”,

*Appl. Phys. Lett.*, vol. 80, pp. 1722 – 1724, 2002). Our computed current density of  $4.4\text{mA/cm}^2$  ( $=55\text{mA}/\pi 2^2$ ) falls between these experimental measurements, indicating a good current prediction capability of our model.

Electric power consumption in the plasma is found to be  $298\text{mW/cm}^3$  from our  
 5 model. This is almost identical to  $300\text{mW/cm}^3$  measured by Massines *et al* (*supra*) and  
 similar to  $277\text{mW/cm}^3$  measured by Chen *et al* (Z. Chen, J. E. Morrison, R. Ben Gadri,  
 and J. R. Roth, “A low-frequency impedance matching circuit for a one atmospheric  
 uniform glow discharge plasma reactor”, paper 6P63, presented at the 25<sup>th</sup> *IEEE*  
*International Conference on Plasma Science*, Raleigh, USA, June 1998). We have also  
 10 calculated electron density and ion density across the space between the two electrodes.  
 The time and spatial variation of electron density is similar to that computed in  
 Massines *et al* (*supra*). A rapid rise of electron density occurs near  $250\mu\text{s}$  and is a result  
 of the gas ionisation (or discharge) in that half cycle ( $250 - 300\mu\text{s}$ ), and the relatively  
 uncharged electron density peak during the remaining period of the half cycle suggests  
 15 a phase of inactive electron production. The peak electron density predicted with our  
 model is  $0.95 \times 10^{10} \text{ cm}^{-3}$ , not very dissimilar to  $2 \times 10^{10} \text{ cm}^{-3}$  by Tochikubo *et al* (*supra*)  
 but much lower than  $30 \times 10^{10} \text{ cm}^{-3}$  calculated by Massines *et al* (*supra*). Again the large  
 electron density reported by Massines *et al* (*supra*) may be a result of their  
 overestimated ionization coefficient for nitrogen (see Figure 1). For diffuse atmospheric  
 20 helium plasmas, there is very little data of direct measurement of electron density for  
 comparison with our calculated electron density. However indirectly the ion-trapping  
 mechanism proposed by Roth (*supra*) may be used to estimate the average electron  
 density and this can be captured by the following equation:

$$n_e = \frac{2mv_e P_{av}}{e^2 E_0^2} \quad (3)$$



where  $n_e$  is the average electron density,  $m$  electron mass,  $e$  electron charge,  $\nu_c$  electron collision frequency in helium,  $P_{av}$  the average electric power density consumed in the plasma, and  $E_0$  the peak electric field in the plasma. Assuming  $P_{av} = 300 \text{ mW/cm}^3$ ,  $E_0 = 3 \text{ kV/cm}$ , and  $\nu_c = 1.8 \times 10^{12} \text{ Hz}$  (see Roth, *supra*), eq.(3) yields  $4.3 \times 10^8 \text{ cm}^{-3}$ . Given

5 that the peak electron density is approximately 10 – 50 times greater than the calculated average electron density, the above calculation suggests that the peak electron density is between  $4 \times 10^9 \text{ cm}^{-3}$  and  $2 \times 10^{10} \text{ cm}^{-3}$ . Thus our calculated peak electron density appears reasonable. This is also confirmed by electron density estimate using the current density formula of  $J = en_e \mu E$  (where  $\mu$  is the electron mobility) as employed for measuring

10 electron density in micro-hollow cathode discharges (see R. H. Stark and K. H. Schoenbach, "Direct current high-pressure glow discharges", *Journal of Applied Physics*, vol. 85, pp. 2075 – 2080, 1999). In general our simulated voltage-current characteristics, the peak discharge current density, the plasma power density, and the electron density yield a favourable comparison with available experimental and

15 numerical data of comparable diffuse atmospheric helium discharges. While there is much scope to include other features of diffuse atmospheric plasmas, for example multi-dimensional effects, our plasma model described above is capable of capturing the main plasma features accurately and as such it will be used to explore the benefits of plasma pulsing.

20

The underlying inventive concept, realising a benefit of energy saving is best understood from the voltage-current characteristic in Figure 2 (Massines *et al*, *supra*). It is seen that the discharge current 6 is of very low magnitude after its peak between  $207 \mu\text{s} - 245 \mu\text{s}$  in the half-cycle from  $200 \mu\text{s}$  to  $250 \mu\text{s}$ , when the applied voltage 4 is

25 very large. This suggests that between the instant of this discharge current pulse and

the polarity reversal point (that occurs at around  $250\mu\text{s}$ ) of the applied voltage 4 in the same half cycle the applied voltage 4 does not necessarily contribute to plasma generation but may adversely heat up electrons. Through energy transfer from electrons to heavy particles, this undesirable electron heating would increase gas temperature.

- 5 Therefore by reducing the applied voltage 4 over this “inactive” period of electron production, the gas temperature may be lowered and equally importantly the input power can be reduced.

### **Description of the Preferred Embodiments**

- 10 We will now describe preferred embodiments of the invention by means of four examples. The first uses a waveform essentially comprising a peak-levelled sinusoid. The second employs a ‘tail-trimmed’ sinusoid, and the third employs a ‘tail-shaped’ sinusoid. The fourth example describes how a control system can be used to shape the waveform of the applied voltage in response to the resultant discharge current.

15

### **Example 1-Peak-Levelled Sinusoid**

- We first consider a simple pulsed excitation voltage waveform, shown in Figure 4a, which is essentially derived from a sinusoidal wave with its peak (positive and negative) levelled to a flat top. Voltage waveform of Figure 4a can be easily obtained
- 20 electronically, and so it represents a realistic option. By reference to Figure 3, the general equation describing the peak-levelled pulse waveform,  $V(t)$ , is as follows:

$$V(t) = \begin{cases} V_m \sin\left(\frac{\pi}{2} - x_1\right) & \left(\frac{\pi}{2} - x_1\right) < \text{rem}(2\pi f t, 2\pi) < \left(\frac{\pi}{2} + x_1\right) , \\ V_m \sin\left(\frac{3\pi}{2} - x_1\right) & \left(\frac{3\pi}{2} - x_1\right) < \text{rem}(2\pi f t, 2\pi) < \left(\frac{3\pi}{2} + x_1\right) , \\ V_m \sin(2\pi f t) & \text{elsewhere} \end{cases}$$

where:

$$0 \leq x_1 \leq \frac{\pi}{2}$$

and:

$\text{rem}(2\pi f t, 2\pi)$  gives the remainder after the division  $(2\pi f t)/2\pi$ .

5

With reference to Figure 4, the magnitude of the original sinusoidal voltage,  $V_s$ , is fixed at 1.5kV, whereas that of the peak-levelled voltage 7,  $V_p$ , varies from 0.4kV to 1.5kV. The repetition frequency of the excitation voltage remains at 10kHz.

Figure 4b shows the voltage and current characteristics of a diffuse nonthermal  
 10 atmospheric gas discharge generated with  $V_p = 1.2\text{kV}$ . The discharge current 8 remains repetitive and stable through many tens of cycles of the applied voltage 7. Therefore under the conditions considered here, pulsing the plasma-generating voltage 7 does not appear to significantly affect the establishment of diffuse nonthermal atmospheric plasma. More specifically the waveform of the discharge current 8 remains relatively  
 15 unchanged from that under the sinusoidal excitation, and the peak current is again around 55 mA very similar to the sinusoidal case of Figure 2.

The basic voltage-current characteristics remain relatively unchanged until  $V_p$  decreases below 750V when the generated plasma becomes unsustainable and eventually extinguishes. This is illustrated in Figure 5 where the normalized electron  
 20 density shown by diamonds 9 and the normalized plasma power density shown by circles 10 are plotted against the normalized magnitude of the applied voltage,  $V_p/V_s$ . The normalizations of electron density and plasma power density in this figure, and in

Figures 6 and 7 are carried out with respect to the electron density and plasma power density obtained by sinusoidal excitation, as illustrated in Figure 2). Lines 11 and 12 are drawn through the electron density data 9 and the plasma power density data 10 respectively, to guide the eye. It is evident that when  $V_p/V_s > 0.5$  plasma pulsing does not significantly affect electron density while the plasma power is reduced by up to 40%. Further numerical simulations suggest that ion densities are also largely unaffected as long as  $V_p/V_s > 0.5$ . Given that electron and ion densities remain approximately the same and that the discharge current and the gas voltage undergo relatively small changes, the basic plasma characteristics should remain relatively unchanged. In other words voltage pulsing in Figure 4 is unlikely to affect adversely plasma-activated applications that rely on the production of electrons or/and ions, yet is capable of considerable power saving.

It is found that the amount of power saving is dependent on that of nitrogen impurities. In the case of very little nitrogen impurities ( $<0.01\%$ ), numerical studies suggest a power saving of more than 50% as indicated in Figure 6. Again such significant power saving is achieved without affecting the production of electrons and ions. Also found is that the power saving is not at the expense of the production of excited neutral species either. With 0.5% nitrogen, Figure 7 shows the normalized density of  $\text{He}(2^3\text{S})$  13 as a function of the  $V_p/V_s$  ratio. It is evident that the trend of the metastable density 13 effectively tracks that of the electron density 14. So if the plasma power is reduced with the electron density 14 kept approximately the same as that with sinusoidal excitation (without pulsing), the metastable density 13 will also remain at approximately the same level as its value with sinusoidal excitation.

The density tracking between electrons and metastables suggests a key role played by electrons in influencing production of excited neutral species in diffuse

atmospheric gas discharges. It is known that energy required to excite neutral species and create chemically reactive species is usually provided through the kinetic energy of electrons. There are also reactive species whose densities are directly proportional to electron density. For example, densities of most oxygen species (e.g. atomic oxygen, singlet-sigma metastable oxygen, singlet-delta metastable oxygen) in a diffuse nonthermal atmospheric discharge in an oxygen-helium mixture are found to be proportional to  $P_{RF}^m$  where  $m = 0.8 - 1.9$  and  $P_{RF}$  is the input RF power to the generated plasma (see J. Y. Jeong, J. Park, I. Henins, S. E. Babayan, V. J. Tu, G. S. Selwyn, G. Ding, and R. F. Hicks, "Reaction chemistry in the afterglow of an oxygen-helium atmospheric plasma", *J. Phys. Chem.*, vol. 104, pp. 8027 – 8032, 2000). According to eq.(3), these oxygen densities are also proportional to electron density. Therefore the very similar electron densities in the sinusoidal case of Figure 2 and the pulsed case of Figure 4 may be a good basis to consider that the densities of most reactive species in the two cases would be similar and so would their chemical reactivity. Thus it is possible to produce at least some reactive species electrically efficiently with voltage pulsing, and as such this will also be useful for applications that rely on reactive species. It is important to note however that in general there is no direct correlation between electron density and densities of all reactive species. There are reactive species whose densities may be inversely proportional to electron density, for example ozone in the oxygen-helium plasma mentioned Jeong *et al* (*supra*). So for individual diffuse nonthermal atmospheric plasmas, the suggested maintenance of production of reactive species deduced from that of electron production needs to be assessed carefully. Our observation is that it is possible for diffuse nonthermal atmospheric plasmas to maintain densities of some reactive species with reduced electric power.

**Example 2-Tail-Trimmed Waveform**

An alternative embodiment to achieve the benefits of the invention may be referred to as a tail-trimmed pulse waveform. With reference to Figure 8, such a waveform may be described by the following equations:

$$V(t) = \begin{cases} V_m \sin\left(\frac{\pi}{2} - x_1\right) & \left(\frac{\pi}{2} - x_1\right) < \text{rem}(2\pi f t, 2\pi) \leq \left(\frac{\pi}{2} + x_1 - x_2\right), \\ V_m \sin\left(\frac{\pi}{2} - x_1\right) \sin(2\pi f' t + \theta) & \left(\frac{\pi}{2} + x_1 - x_2\right) < \text{rem}(2\pi f t, 2\pi) < \pi, \\ V_m \sin\left(\frac{3\pi}{2} - x_1\right) & \left(\frac{3\pi}{2} - x_1\right) < \text{rem}(2\pi f t, 2\pi) \leq \left(\frac{3\pi}{2} + x_1 - x_2\right), \\ V_m \sin\left(\frac{\pi}{2} - x_1\right) \sin(2\pi f' t + \theta) & \left(\frac{3\pi}{2} + x_1 - x_2\right) < \text{rem}(2\pi f t, 2\pi) < 2\pi \\ V_m \sin(2\pi f t) & \text{elsewhere} \end{cases}$$

where:

$$\begin{aligned} 0 &\leq x_1 \leq \frac{\pi}{2} \\ 0 &\leq x_2 \leq 2x_1 \\ T' &= 2\left(\frac{1}{2} - \frac{x_1}{\pi} + \frac{x_2}{\pi}\right) T \\ f' &= \frac{1}{T'} \\ \theta &= \text{ceil}(2f t) \pi \left(1 - \frac{f'}{f}\right) \end{aligned}$$

and where  $\text{ceil}(2f t)$  rounds  $(2f t)$  to the nearest integer towards infinity.

With reference to Figure 9a, the “tail-off” phase of the applied voltage in (between  $25\mu\text{s}$  and  $50\mu\text{s}$ ) may be trimmed to further enhance energy efficiency for plasma generation. The voltage-current characteristics of the induced atmospheric plasma from this waveform are shown in Figure 9b, where 15 is the applied voltage, 16 is the gas voltage, and 17 is the discharge current. It is evident that moderate voltage trimming does not significantly affect the generation and characteristics of induced nonthermal atmospheric plasmas, though the discharge current 17 has different peak values in different half cycles. Numerical studies suggest that further power saving is

possible but very modest, typically a few percent and at best 10% before electron density starts to decrease.

We have so far established that generation of diffuse nonthermal atmospheric plasmas can be made more efficient by altering the waveform of the applied voltage without affecting the basic plasma characteristics.

### Example 3-Tail-Shaped Waveform

In this example, we consider how pulse width may affect plasma generation. In this example we consider one particular type of pulsed voltage signal constructed from a sinusoidal signal for the voltage rise phase and a Gaussian decay for the voltage tail phase. Mathematically in each cycle they may be expressed as follows

$$V(t) = \begin{cases} V_0 \sin \omega t & \text{if } 2N\pi \leq t < t_0 + 2N\pi \\ V_p \exp[-(t - t_0 - 2N\pi)^2 / \tau^2] & \text{if } t_0 + 2N\pi \leq t < 2N\pi + \pi \\ V_0 \sin \omega t & \text{if } 2N\pi + \pi \leq t < t_0 + 2N\pi + \pi \\ -V_p \exp[-(t - t_0 - 2N\pi - \pi)^2 / \tau^2] & \text{if } t_0 + 2N\pi + \pi \leq t < 2N\pi + 2\pi \end{cases} \quad (4)$$

where  $V_0$  is the peak voltage of the sinusoidal signal,  $V_p$  is the peak voltage of the Gaussian decay signal,  $\tau$  is the pulse width of the Gaussian signal,  $\omega = 2\pi/T$  is the angular frequency of the applied voltage with  $T$  being its period, and  $t_0$  the instant at which the sinusoidal and the Gaussian signals joint.  $T_0$  and  $t_0$  are defined as follows:

$$\begin{aligned} T_0 &= \frac{T}{2\pi} \arcsin \left[ \frac{V_p}{V_0} \right] \\ t_0 &= T_0 + kT/2 \\ k &= \text{mod}(t, T/2) \end{aligned} \quad (5)$$

To compare to the sinusoidal case of Figure 2, we set  $V_0 = 1.5\text{kV}$ ,  $V_p = 1.4\text{kV}$ , and  $\tau = T/8$ . The waveform of the applied voltage is shown in Figure 10a, and the voltage and current signals of the generated atmospheric plasma is shown in Figure 10b, where

19 is the applied voltage, 20 is the gas voltage, and 21 is the discharge current. It is evident that the pattern of one discharge every half cycle remains and this is repetitive for many tens of cycles. On the other hand, the gas voltage is markedly different from that in the sinusoidal case of Figure 2. Particularly it has a large hump preceding the main peak that causes the discharge event in each half cycle. Also after the discharge event where the discharge current peaks, the gas discharge does not reduce to zero as rapidly as in the sinusoidal case.

The discharge current 21 is between 30 – 45mA, markedly lower than 55mA calculated for the sinusoidal case. Interestingly the pulse width of the discharge current 21 is much larger than that in the sinusoidal case (Figure 2), particularly for the positive half cycles. For the case in Figure 10, electric power density consumed in the plasma is about  $0.32\text{W/cm}^3$ , about 7% above that in the sinusoidal case. Further numerical examples studied suggest that under other pulsing conditions diffuse atmospheric helium plasmas excited with the pulsed voltage of Figure 10a consume approximately the same amount of electric power as those with sinusoidal excitation. Therefore shortening the pulse width may not be as effective in achieving energy saving on an absolute basis, but, as discussed below, have advantages in energy-saving for a given density of electrons and metastables achieved. From the voltage-current characteristic, this is likely due to the wider pulse widths for both the discharge current and the gas voltage. On the other hand, electron density achievable can be much higher. For the case shown in Figure 10b, the peak electron density is found to be  $1.74 \times 10^{10}\text{cm}^{-3}$ , 83% above  $0.95 \times 10^{10}\text{cm}^{-3}$  for the sinusoidal case. The spatial variation of electron density over one half cycle shows a similar distribution to that that produced by the sinusoidal waveform presented above yet with clear difference near the voltage polarity reversal point. There is a clear evidence of pulsed production of electrons. Further numerical



calculations suggest that by changing the pulse width of the applied voltage in Figure 10a, electron and metastable densities can be made much greater than that under sinusoidal excitation. Though inappropriate wave-shaping of the applied voltage can also reduce electron and metastable densities, the above discussions suggest that through control of pulse width it is possible to enhance production of electrons and metastables for a given plasma power consumption. To see this more clearly, we calculate the ratio of electron density to plasma power density (number of electrons that can be produced at a given input power). This is  $5.4 \times 10^{10}/W$  for this example, and  $3.2 \times 10^{10}/W$  for the sinusoidal waveform presented above, an improvement of 68%. From this comparison, it is still electrically efficient to pulse the applied voltage for the generation of diffuse nonthermal atmospheric plasmas.

#### **Example 4 – Controlled Waveform**

It is clear that an optimal saving of energy in the production of gas plasmas may be obtained by the use of a control system, such as a feedback control system, wherein the waveform of the applied voltage is driven by the control system, which itself uses the discharge current as an input variable. In this way, the voltage signal may be attenuated following the plasma discharge, so as to make most efficient use of the input energy. The use of such a control system can then also take account of any temporal changes in the system configuration (such as changes in electrode or dielectric coating characteristics, or changes in the gas composition), leading to waveforms (as defined herein) that may vary in their repetition rate, and which may vary in peak shape and amplitude from cycle to cycle.

**Parametric Ranges of Key System Variables**

*Electrode size:* Typically between  $50\text{cm}^2$  and  $100\text{cm}^2$  of either circular or rectangular shapes. Scaling up is possible, with the electrode area divided into different sections connected in parallel to the supply power source. To control plasma stability with large  
5 electrodes, it may be useful to use individually valued series resistors or impedance networks in each of these parallel circuit branches. On the other hand, plasma stability is easier to achieve with smaller electrodes than  $50\text{cm}^2$ .

*Electrode separation:* Typically around 1cm. Smaller electrode separation makes it easier to control plasma stability. Although larger electrode separation tends to un-  
10 stabilise the generated nonthermal plasma, it is quite possible to increase the electrode separation up to tens of centimetres, especially when the electrode area is large and the electric power pulsed.

*Capacitance of dielectric coatings:* For the case where at least one of the electrodes has a dielectric coating, their capacitance depends on the size of the electrodes and hence  
15 that of the dielectric. Typically for a surface area of  $10\text{cm}^2$  the capacitance of one dielectric coating is between 10pF and 100pF. If the surface area of the dielectric coatings is increased, the capacitance increases proportionally. Also it is equally acceptable to coat either one electrode or both electrodes, the latter of which will have the coating capacitance halved.

*Peak voltage:* This depends on the repetition frequency, the electrode separation, and gas composition. At a repetition frequency of 10kHz and an electrode separation of 0.5cm, the peak voltage needs to be greater than 1.0kV but usually less than 2kV in helium or helium mixed with a small fraction of nitrogen or/and oxygen (typically less than 1%). This needs to be increased when the electrode separation is increased. At a  
25 greater repetition frequency on the other hand, the peak voltage required becomes

smaller. For example between 10 and 20MHz, the peak voltage can be reduced to as low as 500V in helium with 0.5cm electrode separation.

*Gas composition:* Our numerical work was performed for helium-nitrogen mixture. For applications, helium-oxygen is more useful and argon-oxygen is even better as argon is cheaper than helium. The most practically convenient gas is air (though very difficult to simulate). Alternatively noble gases mixed with a small fraction of a reactive gas (such as, but not limited to, oxygen can be used.

*$t_0$  in the Gaussian decay function:*  $t_0$  is given in equation 4 and 5 in Example 3 of the preferred embodiments. Typically it is between 5% and 15% of the repetition period of the applied electric voltage.

### Summary

Diffuse nonthermal gas discharges generated at atmospheric pressure have found increasing applications in many key materials processing areas such as etching, deposition, and structural modification of polymeric surfaces. To facilitate tailored and improved applications of these novel gas plasmas, we consider their pulsed generation based on one-dimensional numerical simulation of helium-nitrogen discharges. We consider four waveforms of the plasma-generating voltage, namely (1) sinusoidal; (2) peak-levelled sinusoidal; (3) peak-levelled and tail-trimmed sinusoidal; and (4) pulsed with a Gaussian-shaped tail, all at the same repetition frequency of 10kHz. For each case, voltage and current characteristics are calculated and then used to assess whether the generated plasma is diffuse and nonthermal. Densities of electrons, ions, and metastables are calculated, together with the dissipated electric power in the plasma bulk. It is found that plasma pulsing can significantly reduce the electric power needed to sustain diffuse nonthermal

atmospheric plasmas. Specifically by choosing appropriate pulse shape, the plasma-sustaining power can be reduced by more than 50% without reducing densities of electrons, ions, and metastables. On the other hand, electron density can be enhanced by 68% with the same input electric power if the pulse width is suitably  
 5 narrowed.

### Scope of the Invention

The invention is defined in the Claims, which now follow, and in which the term “waveform” is understood to include periodic signals that have a zero value over  
 10 more than an instantaneous part of the period, and which are more commonly referred to as “pulse trains”.

In the Claims, the term “truncated” is taken to include limited in amplitude to a maximum and/or minimum voltage, such limitation typically leading to a waveform with a substantially flat profile at its extreme value or values, and/or to include  
 15 narrowed in pulse width.

In the Claims, Equation E1 is taken to be:

$$V(t) = \begin{cases} V_m \sin\left(\frac{\pi}{2} - x_1\right) & \left(\frac{\pi}{2} - x_1\right) < \text{rem}(2\pi f t, 2\pi) < \left(\frac{\pi}{2} + x_1\right) , \\ V_m \sin\left(\frac{3\pi}{2} - x_1\right) & \left(\frac{3\pi}{2} - x_1\right) < \text{rem}(2\pi f t, 2\pi) < \left(\frac{3\pi}{2} + x_1\right) , \\ V_m \sin(2\pi f t) & \text{elsewhere} \end{cases}$$

where:

$$0 \leq x_1 \leq \frac{\pi}{2}$$

and:

20

$\text{rem}(2\pi f t, 2\pi)$  gives the remainder after the division  $(2\pi f)/2\pi$ .

and further, **Equation E2** is taken to be:

$$V(t) = \begin{cases} V_m \sin\left(\frac{\pi}{2} - x_1\right) & \left(\frac{\pi}{2} - x_1\right) < \text{rem}(2\pi f t, 2\pi) \leq \left(\frac{\pi}{2} + x_1 - x_2\right), \\ V_m \sin\left(\frac{\pi}{2} - x_1\right) \sin(2\pi f' t + \theta) & \left(\frac{\pi}{2} + x_1 - x_2\right) < \text{rem}(2\pi f t, 2\pi) < \pi, \\ V_m \sin\left(\frac{3\pi}{2} - x_1\right) & \left(\frac{3\pi}{2} - x_1\right) < \text{rem}(2\pi f t, 2\pi) \leq \left(\frac{3\pi}{2} + x_1 - x_2\right), \\ V_m \sin\left(\frac{\pi}{2} - x_1\right) \sin(2\pi f' t + \theta) & \left(\frac{3\pi}{2} + x_1 - x_2\right) < \text{rem}(2\pi f t, 2\pi) < 2\pi \\ V_m \sin(2\pi f t) & \text{elsewhere} \end{cases}$$

where:

$$0 \leq x_1 \leq \frac{\pi}{2}$$

$$0 \leq x_2 \leq 2x_1$$

$$T' = 2 \left( \frac{1}{2} - \frac{x_1}{\pi} + \frac{x_2}{\pi} \right) T$$

$$f' = \frac{1}{T'}$$

$$\theta = \text{ceil}(2 f t) \pi \left( 1 - \frac{f'}{f} \right)$$

a

nd where  $\text{ceil}(2 f t)$  rounds  $(2 f t)$  to the nearest integer towards infinity.

5 and **Equation E3** is taken to be:

$$V(t) = \begin{cases} V_0 \sin \omega t & \text{if } 2N\pi \leq t < t_0 + 2N\pi \\ V_p \exp\left[-(t - t_0 - 2N\pi)^2 / \tau^2\right] & \text{if } t_0 + 2N\pi \leq t < 2N\pi + \pi \\ V_0 \sin \omega t & \text{if } 2N\pi + \pi \leq t < t_0 + 2N\pi + \pi \\ -V_p \exp\left[-(t - t_0 - 2N\pi - \pi)^2 / \tau^2\right] & \text{if } t_0 + 2N\pi + \pi \leq t < 2N\pi + 2\pi \end{cases}$$

In all of which equations E1, E2 and E3, the parameters are to be interpreted as described herein.